Clustering Algorithms

- Partitional clustering
- Hierarchical clustering
- Density-based clustering
- Graph-based clustering

© Tan,Steinbach, Kumar

Introduction to Data Mining

4/18/2004

4/18/2004

K-means Clustering

- Partitional clustering approach
- Each cluster is associated with a centroid (center point)
- Each point is assigned to the cluster with the closest centroid
- Number of clusters, K, must be specified
- The basic algorithm is very simple
- 1: Select K points as the initial centroids.
- Form K clusters by assigning all points to the closest centroid.
- Recompute the centroid of each cluster.
- 5: until The centroids don't change

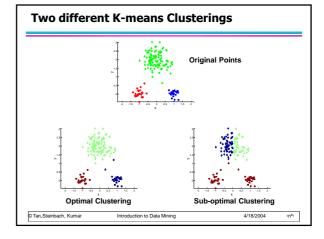
Tan,Steinbach, Kumar Introduction to Data Mining

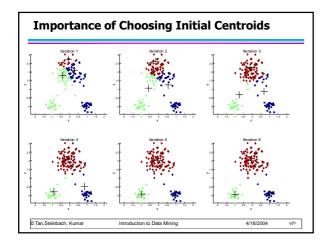
4/18/2004

K-means Clustering - Details

- Initial centroids are often chosen randomly.
 - Clusters produced vary from one run to another
- The centroid is (typically) the mean of the points in the
- 'Closeness' is measured by Euclidean distance, cosine similarity, correlation, etc.
- K-means will converge for common similarity measures mentioned above.
- Most of the convergence happens in the first few iterations.
 - Often the stopping condition is changed to 'Until relatively few points change clusters'
- Complexity is O(n * K * I * d)
 - $$\begin{split} n &= \text{number of points, K} = \text{number of clusters,} \\ I &= \text{number of iterations, d} = \text{number of attributes} \end{split}$$

Introduction to Data Mining





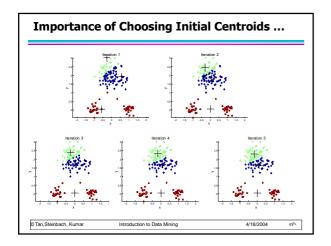
Evaluating K-means Clusters

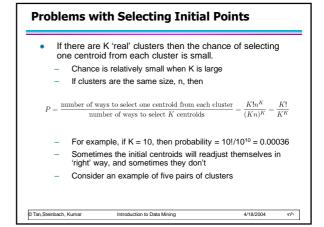
- Most common measure is Sum of Squared Error (SSE)
 - For each point, the error is the distance to the nearest cluster
 - To get SSE, we square these errors and sum them.

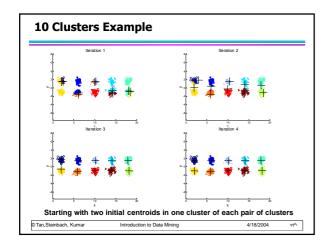
$$SSE = \sum_{i=1}^{K} \sum_{j=0}^{K} dist^{2}(m_{i}, x)$$

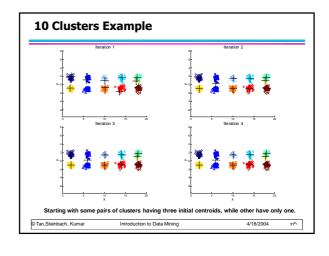
- x is a data point in cluster C_i and m_i is the representative point for
- can show that m_i corresponds to the center (mean) of the cluster
- Given two clusters, we can choose the one with the smallest
- One easy way to reduce SSE is to increase K, the number of
 - ◆ A good clustering with smaller K can have a lower SSE than a poor clustering with higher K

Introduction to Data Mining









Solutions to Initial Centroids Problem

- Multiple runs
 - Helps, but probability is not on your side
- Sample and use hierarchical clustering to determine initial centroids
- Select more than k initial centroids and then select among these initial centroids
 - Select most widely separated
- Postprocessing
- Bisecting K-means
 - Not as susceptible to initialization issues

Tan, Steinbach, Kumar Introduction to Data Mining 4/18/2004 (nº)

Handling Empty Clusters

- Basic K-means algorithm can yield empty clusters
- Several strategies
 - Choose the point that contributes most to SSE
 - Choose a point from the cluster with the highest SSE
 - If there are several empty clusters, the above can be repeated several times.

© Tan, Steinbach, Kumar Introduction to Data Mining 4/18/2004 (n°)

Updating Centers Incrementally

- In the basic K-means algorithm, centroids are updated after all points are assigned to a centroid
- An alternative is to update the centroids after each assignment (incremental approach)
 - Each assignment updates zero or two centroids
 - More expensive
 - Introduces an order dependency
 - Never get an empty cluster
 - Can use "weights" to change the impact

© Tan, Steinbach, Kumar

Introduction to Data Mining

4/18/2004

4/18/2004

Pre-processing and Post-processing

- Pre-processing
 - Normalize the data
 - Eliminate outliers
- Post-processing
 - Eliminate small clusters that may represent outliers
 - Split 'loose' clusters, i.e., clusters with relatively high SSE
 - Merge clusters that are 'close' and that have relatively low SSE
 - Can use these steps during the clustering process
 ISODATA

Tan, Steinbach, Kumar Introduction to Data Mining

4/18/2004

4/18/2004

Bisecting K-means

- Bisecting K-means algorithm
 - Variant of K-means that can produce a partitional or a hierarchical clustering
- 1: Initialize the list of clusters to contain the cluster containing all points.
- 2: repea
- 3: Select a cluster from the list of clusters
- for i = 1 to number_of_iterations do
 Bisect the selected cluster using basic K-means
- 6: end for
- 7: Add the two clusters from the bisection with the lowest SSE to the list of clusters.
- 8: until Until the list of clusters contains K clusters

Tan, Steinbach, Kumar Introduction to Data Mining

Limitations of K-means

- K-means has problems when clusters are of differing
 - Sizes
 - Densities
 - Non-globular shapes
- K-means has problems when the data contains outliers.

Steinbach, Kumar Introduction to Data Mining

